

# Shape coexistence in neutron deficient mercury isotopes

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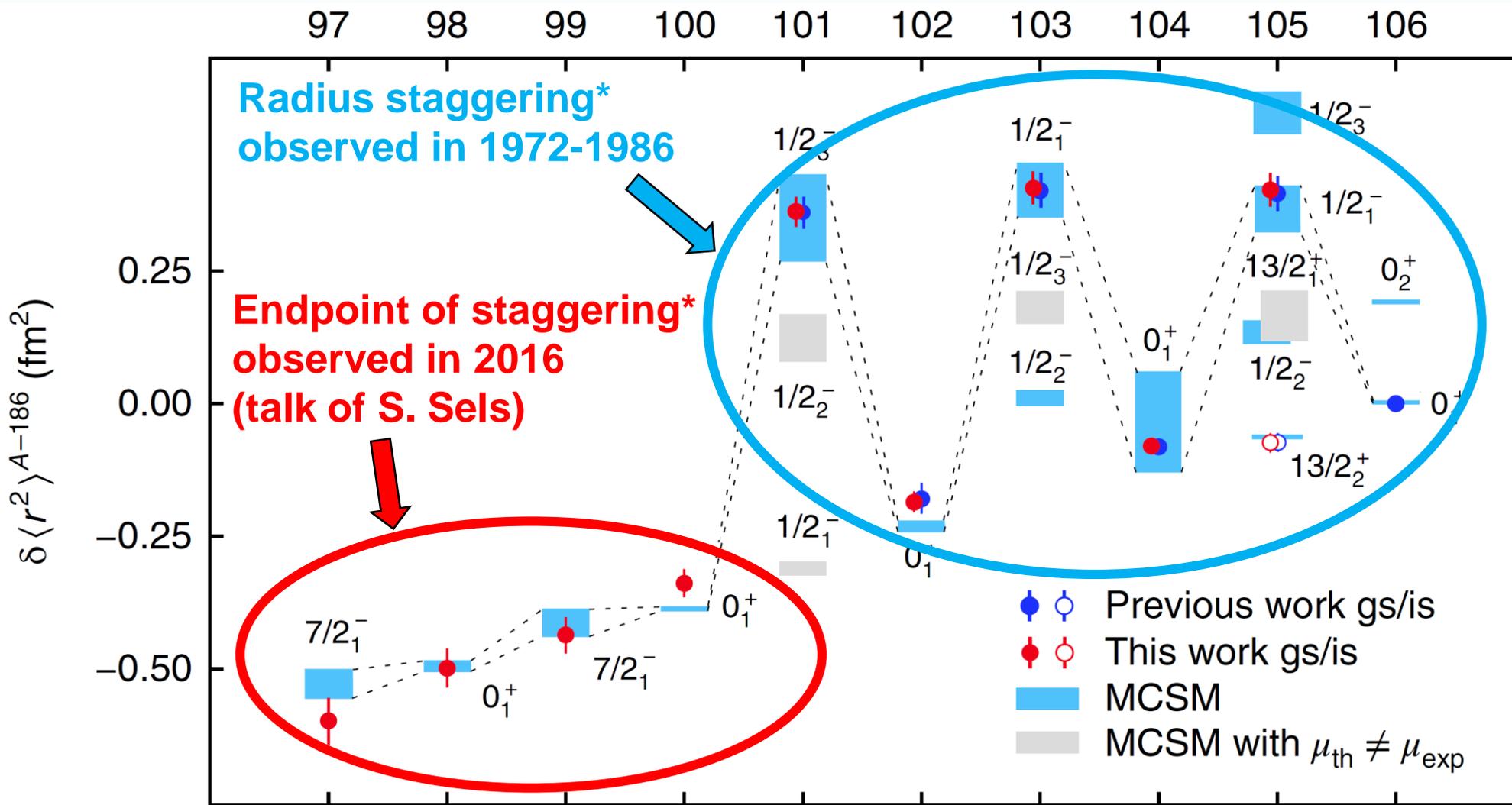
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[1] B.A. Marsh et al. Nature Physics 14 (2018) 1163

[2] S. Sels et al., Phys. Rev. C 99 (2019) 044306

**\*A much weaker odd-even radius staggering is an ubiquitous phenomenon observed in most of the isotopic chains This talk is about a giant radius staggering observed only in the chain of light mercury isotopes.**



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# The physics of radius staggering in Hg

J. Bonn et al., Phys. Lett. B 38, 308 (1972).

*“The observation of the anomalous isotopic shift in  $^{183,185}\text{Hg}$  points to the possible existence of a new region of strongly deformed nuclei only two units away from the closed proton shell.”*

G. Ulm et al., Z. Phys. A: At. Nucl. 325, 247 (1986).

*“Now it is widely accepted that the light even Hg isotopes, as well as  $^{185m}\text{Hg}$ , and those with  $A > 186$  have a small oblate deformation, while the light odd isotopes  $^{181}\text{Hg}$ ,  $^{183}\text{Hg}$ , and  $^{185}\text{Hg}$  are strongly deformed and prolate.”*



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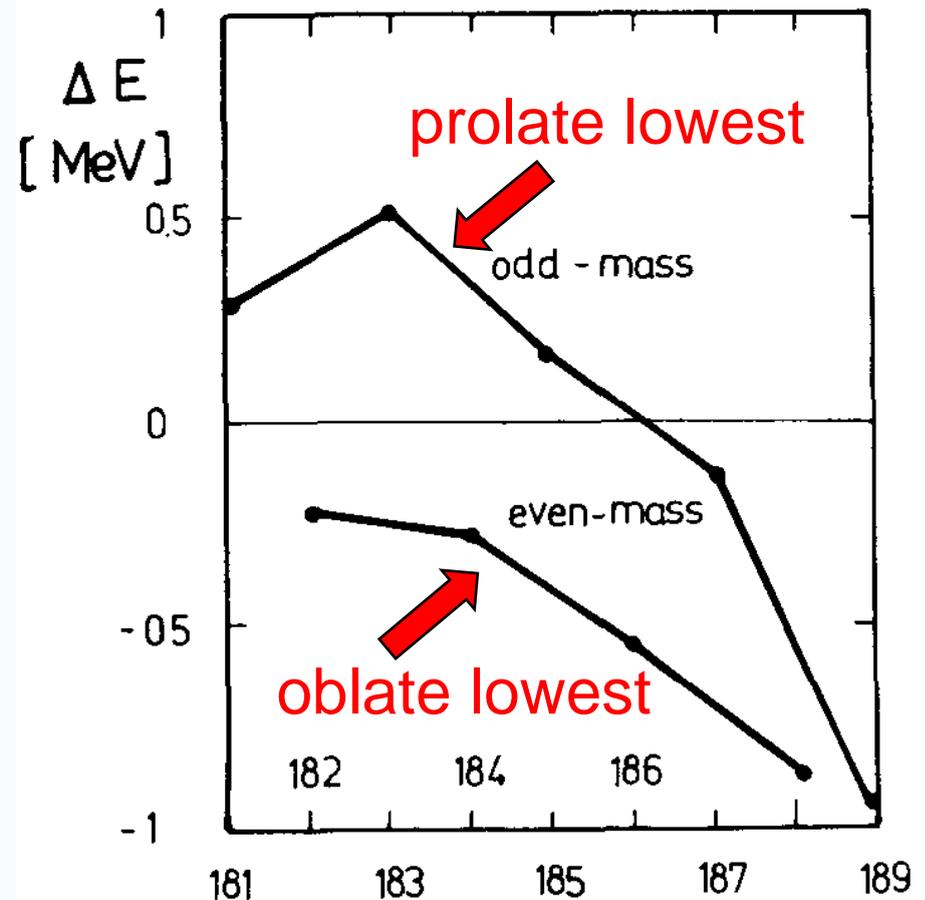
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# Theoretical description of radius staggering in Hg

S. Frauendorf and V. V. Pashkevich, Phys. Lett. B 55, 365 (1975).

*“A more critical point, however, is the proper choice of the strength of the pairing interaction because the energy difference between the two minima  $\Delta E$  sensitively depends on this quantity. [...] Therefore it is very difficult to obtain  $\Delta E$  with the required accuracy and we allowed for a certain adjustment of  $\Delta E$  via the averaged proton gap.”*



# Nuclear DFT description of radius staggering in Hg

- [1] S. Sakakihara and Y. Tanaka, Nuclear Phys. A 726, 37 (2003).
- [2] J. M. Yao et al., Phys. Rev. C 87, 034322 (2013).
- [3] J. M. Boillos and P. Sarriguren, Phys. Rev. C 91, 034311 (2015).
- [4] V. Manea et al., Phys. Rev. C 95, 054322 (2017).
- [5] S. Sels et al., Phys. Rev. C 99, 044306 (2019).**

**In [5] we say:**

*“Early DFT calculations for both even- and odd-mass isotopes mercury isotopes [...] achieved a reproduction of the odd-even radius staggering for  $N > 100$  by fitting the pairing strength to the one-particle separation energy of these isotopes [2]. In Ref. [3] the shape coexistence in the region was confirmed as a mechanism for the observed radius staggering. [...] As explicitly noted in Ref. [4], the precise staggering pattern depends sensitively on the details of the effective interaction.”*



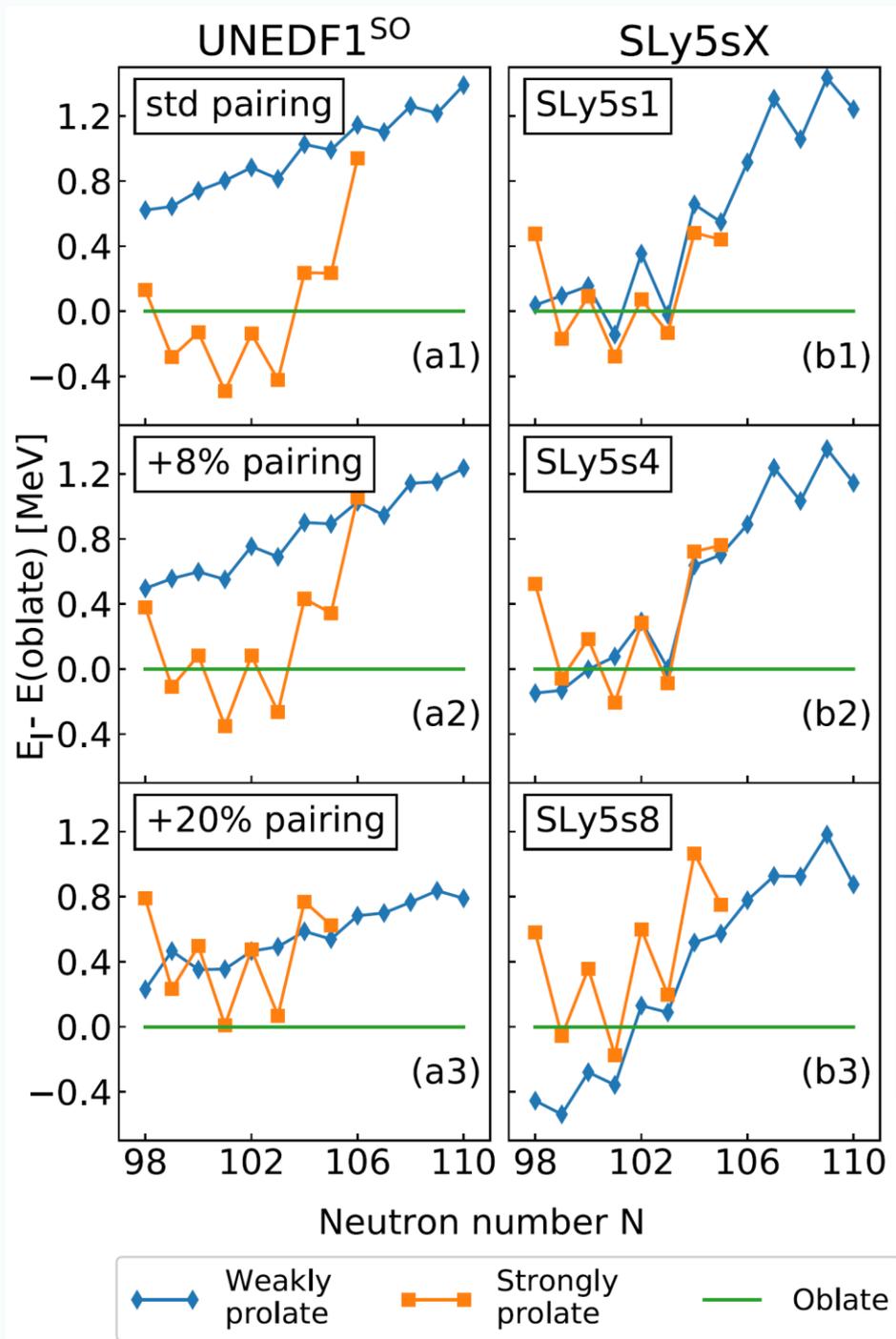
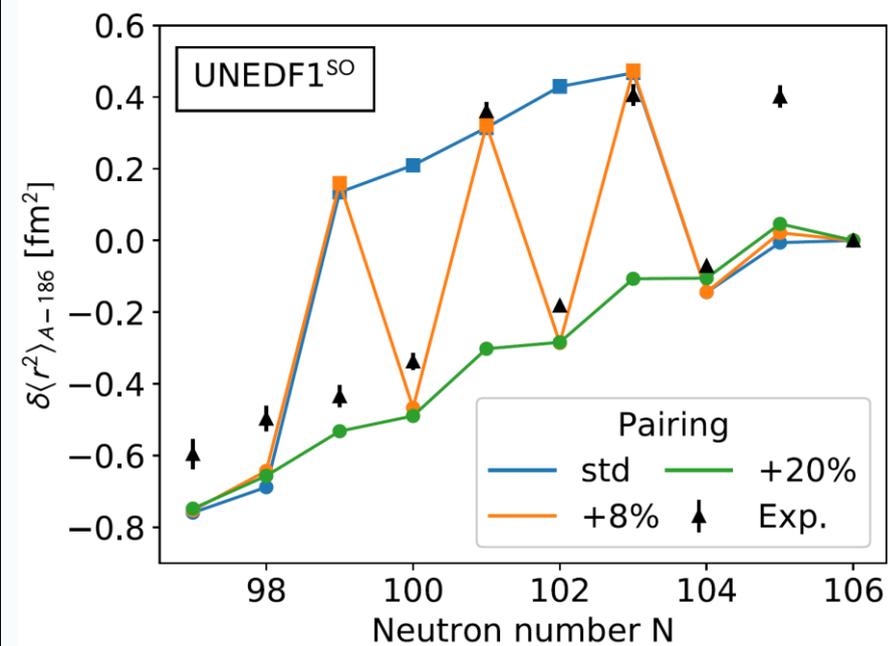
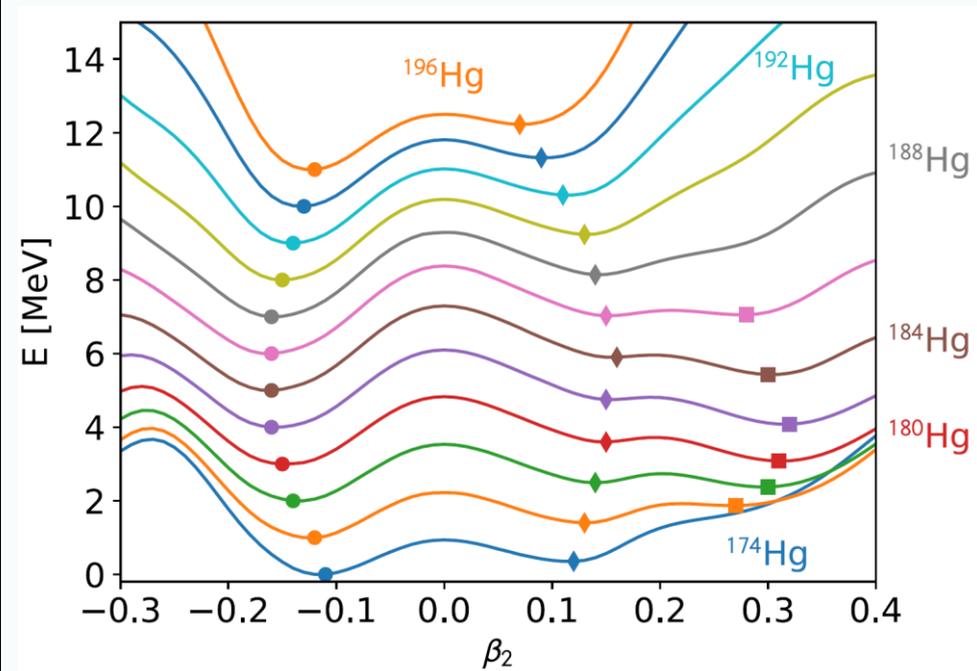
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S. Sels et al., Phys. Rev. C 99, 044306 (2019).



# Conclusions

1. Fantastically precise laser spectroscopy measurements have revealed spectacular phenomenon of a **giant charge radius staggering in three odd mercury isotopes**  $^{191}\text{Hg}$ ,  $^{193}\text{Hg}$ , and  $^{195}\text{Hg}$ , whereas all other isotopes between  $A=177$  and  $A=126$  follow a typical, fairly smooth behaviour.
2. Already in 1975, this phenomenon was correctly associated and properly described in terms of the **quadrupole shape staggering** between weakly oblate and strongly prolate deformations. This interpretation still holds today.
3. Numerous later DFT studies and the latest tour-de-force MCSM study have **confirmed this interpretation**.
4. Detailed description of energies of the competing shapes would require an **unprecedented and unrealistic precision** of modelling below 100 keV. This level of precision is possible only by an extreme fine-tuning of model parameters.



# Thank you



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# MCSM description of radius staggering

B.A. Marsh et al., Nature Physics 14 (2018) 1163

*“This work represents the largest ever MCSM calculations, performed on massively parallel supercomputers, including the K computer in Kobe, Japan. Exploiting the advantages of quantum Monte-Carlo, variational and matrix-diagonalization methods, this approach circumvents the diagonalization of a  $> 2 \times 10^{42}$ -dimensional Hamiltonian matrix. Using the doubly-magic  $^{132}\text{Sn}$  nucleus as an inert core, 30 protons and up to 24 neutrons were left to actively interact in an exceptionally large model space as compared to conventional CI calculations. Single-particle energies were set to be **consistent** with single particle properties of  $^{132}\text{Sn}$  and  $^{208}\text{Pb}$  with smooth changes as functions of  $Z$  and  $N$ . All nucleons interact through effective NN interactions **adopted** from the frequently-used ones.”*



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